



**Ontario eSecondary School  
Course Outline  
2020-2021**

<b>Ministry of Education Course Title: Mathematics for College Technology</b>	
<b>Ministry Course Code: MCT4C</b>	
<b>Course Type: College Preparation</b>	
<b>Grade: 12</b>	
<b>Credit Value: 1.0</b>	
<b>Prerequisite(s): Functions and Applications, Grade 11, University/College Preparation, or Functions, Grade 11, University Preparation</b>	
<b>Department: Mathematics</b>	
<b>Course developed by: Kiran Sandhar</b>	<b>Date: March 1, 2020</b>
<b>Length: One Semester</b>	<b>Hours: 110</b>
<p>This course has been developed based on the following Ministry documents:</p> <ol style="list-style-type: none"> <li><i>The Ontario Curriculum, Grades 11 and 12 Mathematics, Revised 2007</i></li> <li><i>Growing Success: Assessment, Evaluation, and Reporting in Ontario Schools (2010)</i></li> </ol>	

## **COURSE DESCRIPTION/RATIONALE**

This course enables students to extend their knowledge of functions. Students will investigate and apply properties of polynomial, exponential, and trigonometric functions; continue to represent functions numerically, graphically, and algebraically; develop facility in simplifying expressions and solving equations; and solve problems that address applications of algebra, trigonometry, vectors, and geometry. Students will reason mathematically and communicate their thinking as they solve multi-step problems. This course prepares students for a variety of college technology programs.

## **OVERALL CURRICULUM EXPECTATIONS**

### **Unit 1 & 2:**

By the end of this course, students will:

- solve problems involving exponential equations graphically, including problems arising from real-world applications;
- solve problems involving exponential equations algebraically using common bases and logarithms, including problems arising from real-world applications.

### **Unit 3:**

By the end of this course, students will:

- recognize and evaluate polynomial functions, describe key features of their graphs, and solve problems using graphs of polynomial functions;
- make connections between the numeric, graphical, and algebraic representations of polynomial functions;
- solve polynomial equations by factoring, make connections between functions and formulas, and solve problems involving polynomial expressions arising from a variety of applications.

### **Unit 4:**

By the end of this course, students will:

- determine the values of the trigonometric ratios for angles less than  $360^\circ$ , and solve problems using the primary trigonometric ratios, the sine law, and the cosine law;
- make connections between the numeric, graphical, and algebraic representations of sinusoidal functions;
- demonstrate an understanding that sinusoidal functions can be used to model some periodic phenomena, and solve related problems, including those arising from real-world applications

### **Unit 5:**

By the end of this course, students will:

- represent vectors, add and subtract vectors, and solve problems using vector models, including those arising from real-world applications;
- solve problems involving two-dimensional shapes and three-dimensional figures and arising from real-world applications;
- determine circle properties and solve related problems, including those arising from real-world applications.

## COURSE CONTENT

<i>Unit</i>	<i>Length</i>
<b>1: Exponential Functions</b>	19 hours
<b>2: Logarithmic Functions</b>	18 hours
<b>3: Polynomial Functions</b>	18 hours
<b>4: Trigonometric Functions</b>	25 hours
<b>5: Vectors and Applications of Geometry</b>	20 hours
<b>Culminating Project</b>	8 hours
<b>Final Exam</b>	2 hours
<b>TOTAL</b>	110 hours

## UNIT DESCRIPTIONS

### Unit 1 & 2- Exponential and Logarithmic Functions

Through models, students are introduced to the definition of an exponential function and the notations associated with it. Students use graphing technology and paper-and-pencil tasks to investigate the properties of exponential functions. Students explore the domain and range of functions. Students investigate properties of exponential functions and logarithmic functions. The relationship between exponential function and logarithmic function is explored both algebraically and graphically. Students use laws of logarithms to simplify and evaluate logarithmic expressions, and to solve problems. A variety of models are examined.

### Unit 3 - Polynomial functions

Students are introduced to the main concepts of graphing polynomial functions in order to explore them. Later in the course. Students examine the type and numbers of intercepts, the effect of changing coefficients, symmetry and the degree in relation to the shape of the functions. Using skills from previous years, students explore curve sketching from a factored form. Students will explore polynomial equations. Real and complex roots of both factorable and non-factorable polynomials are determined through graphical investigation and algebraic manipulation. Finally, students will solve problems that involve functions arising from real-world applications.

## **Unit 4- Trigonometric Functions**

Students investigate the periodic nature and graphical properties of the primary trigonometric functions. Students use the primary trigonometric ratios, the sine law, and the cosine law to model and solve triangles. Students investigate the relationship between degree and radian measure, and explore the use of the unit circle and special triangles to determine selected values of the primary trigonometric ratios. Students consolidate and extend concepts first introduced. Using technology, students explore the effects of simple transformations on their graphs and equations. Students apply these concepts to model authentic and real-world problems. Students develop the skills to manipulate and solve trigonometric equations

## **Unit 5 - Vectors and Applications of Geometry**

Students will investigate, and then solve real-world problems. They will demonstrate an understanding of vectors, two-dimensional, three-dimensional in a variety of ways, including circle and related problems

## **TEACHING AND LEARNING STRATEGIES**

**The students will experience a variety of activities:**

### **Whole-Class Activities (facilitated through discussion forums)**

Whole class activities are designed to introduce concepts and skills that are directly applicable to the workplace and to build on the content being studied during small group and individual activities. These activities include the following:

**Teacher demonstrations** through video conferencing, email, or videos provided of a teacher or student demonstrating the concepts and skills being studied. This helps the student and teacher create an atmosphere of trust and respect to aid in the online learning environment.

**Video presentations** and technological aids with videos embedded to enrich the course content and clarify concepts and skills being studied. Also the use of online pre-approved quizzes and games to help a student become more familiar with the concepts and skills being studied.

**Diagnostic and review activities** (audio and video recordings) can be student-lead or teacher lead to work as a review for students through audio and video made to share among each other to help reinforce the concepts and skills being studied.

### **Small Group Activities**

The teacher sets up small group activities to provide opportunities for active and oral learning as well as to bolster practical communication and teamwork skills. The teacher plays a critical role during group activities by monitoring group progress as well as answering questions that arise and using questions to

assist students in their understanding. In this way, the teacher also facilitates student understanding of effective learning, communication, and team building during group activities.

**The small group activities include the following:**

**Paired or small group research activities** students are able to share their work online with not only their teachers, but their classmates too. Students are able to share resources through online chat and video conferencing. The ability to learn from each other, work on teamwork skills, and practice communication are valued and encouraged throughout the course.

**Comparison and evaluation of written work** is very important in this course. This course focuses on giving many examples of correct work, and helping students build the skills needed to peer-correct and self-correct. Students are given a variety of texts to read through embedded links, to make comparisons with different texts, real life situations, and their own writing.

**Practical extension and application of knowledge** is used as an effective learning strategy in this course because it allows the students to read and listen to the texts and stories and reflect back with connections to themselves, other texts and the world. Students are encouraged to share their understandings through work submitted each day, phone conversations about course work, or videoconferencing.

**Oral presentations** in an online environment we have the equipment to have student either live video conference oral presentations, or make videos and submit them for their oral presentations. These oral presentations can be viewed by fellow students (when appropriate) and the teacher. Students can learn from one another, and from their teacher. Such activities include dramatic readings and performances.

**Charts and graphs** are used to present effective learning opportunities of concepts and skills to students who would benefit from visual objects to learn. Every student learns differently, and it is used to help students discover another way to present their information such as graphic organizers, lists, and pictures.

**Individual Activities**

The teacher should provide a variety of individual assignments to expand and consolidate the learning that takes place in the whole-class and small group activities. Individual activities allow the teacher to accommodate interests and needs and to access the progress of individual students. The teacher plays an important role in supporting these activities through the provision of ongoing feedback to the students, both orally and in writing. Teachers are encouraged to include individual activities such as the following in the course:

**Research** is completed in an online environment by teaching the students first about plagiarism rules and giving examples of good sources to use. The students are not only limited to the online search for information, but have resources available by links on the Moodle page of information that has been scanned and uploaded.

**Individual assignments** are worked on at a student's own pace. The teacher can support the student in these activities with ongoing feedback.

**Oral presentations** are facilitated through the use of video conferencing and video recording.

**Practical extension and application of knowledge** helps students develop their own voice, and gives them the ability to make personal connections, and connections to the world throughout their course. Students are given a variety of reading and viewing texts to give them many chances to apply their new concepts, skills, and knowledge.



**Ongoing project work** is something that is valued in the earning of an English credit. The ongoing project can be submitted to the teacher for ongoing feedback in both written and oral work.

## **ASSESSMENT, EVALUATION, AND REPORTING**

**Assessment:** The process of gathering information that accurately reflects how well a student is achieving the identified curriculum expectations. Teachers provide students with descriptive feedback that guides their efforts towards improved performance.

**Evaluation:** Assessment of Learning focuses on Evaluation which is the process of making a judgement about the quality of student work on the basis of established criteria over a limited, reasonable period of time.

**Reporting:** Involves communicating student achievement of the curriculum expectations and Learning Skills and Work Habits in the form of marks and comments as determined by the teacher's use of professional judgement.

## **STRATEGIES FOR ASSESSMENT**

Assessment practices can nurture students' sense of progress and competency and information instruction. Many diagnostic tools, e.g. checklists, are used at regular intervals throughout the units to encourage students' understanding of their current status as learners and to provide frequent and timely reviews of their progress. Assessment of student acquisition of learning skills also occurs regularly through unobtrusive teacher observation and conferencing.

Teachers are encouraged to share goals with students early in the course and to connect unit learning experiences frequently and explicitly with big ideas, overall expectations, and performance tasks. The teacher is encouraged to involve students in the discussion, modification, or creation of rubrics, and teach students to use rubrics as a learning tool..

## **ASSESSMENT ACTIVITIES**

- Homework assignments
- Individual conference meetings
- Diagnostic tests and writing tasks
- Completed Templates & Graphic Organizers
- Reflections
- Oral presentations & Active Listening
- Tests & Exam
- Evaluations

## **EVALUATION**

The final grade will be determined as follows:

- 70% of the grade will be based on evaluation conducted throughout the course. This portion of the grade should reflect the student's most consistent level of achievement throughout the course, although special consideration will be given to more recent evidence of achievement.

- 30% of the grade will be based on a final evaluation administered at or towards the end of the course. This evaluation will be based on evidence from one or a combination of the following: an examination, a performance, and/or another method of evaluation suitable to the course content. The final evaluation allows the student an opportunity to demonstrate comprehensive achievement of the overall expectations for the course.

(*Growing Success: Assessment, Evaluation and Reporting in Ontario Schools*. Ontario Ministry of Education Publication, 2010 p.41)

<b>Weight</b>	
<b>Course Work</b>	<b>70</b>
Knowledge/Understanding	20
Thinking/Inquiry	15
Communication	15
Application	20
<b>Final</b>	<b>30</b>
Exam	20
Culminating Project	10

### **TERM WORK EVALUATIONS (70%):**

Evaluation Item	Description	Category	Weight Factor (1-10)
Reflective research projects	Research-based projects for each unit based on applications of learned functions to real life problems	K,T,C,A	7
Problem sets Learning Logs	Problem sets supplement lessons and are used to assess whether or not students are meeting criteria for success	K,T,C	5
Simulations/Live interview evaluations	Live interviews are used to evaluate students through observation and conversation. Some of these are a part of other research projects.	K,T,C,A	5
Unit Test(s)	Unit tests are based on curriculum expectations and cover the entirety of each unit	K,T,C,A	10

## FINAL EVALUATIONS (30%):

Evaluation Item	Description	Category
Final Exam 20%	A final, written examination, covering all curriculum expectations for the course.	K,T,C,A
Culminating Project 10%	A comprehensive project, covering all overall curriculum expectations for the course.	K,T,C,A

## AFL/AAL/AOL Tracking sheet:

### Unit 1: Exponential Functions

AAL	AFL	AOL
Lesson 0.1 Note-Taking	0.1 Grade 11 Review Student	How to Survive a Zombie Apocalypse
Lesson 1.1 Note-Taking	1.1 Exponent Laws and Rational Exponents	
Lesson 1.2 Note-Taking	1.2 Properties of Exponential Functions	
Lesson 1.3 Note-Taking	1.3 Solving for Exponential Functions using Common Bases	
Lesson 1.4 Note-Taking	1.4 Applications of Exponential Functions	

### Unit 2: Logarithmic Functions

AAL	AFL	AOL
Lesson 2.1 Note-Taking	Investigation 2.1 Inverse Functions-Exponential and Logarithmic	Learning Log
Lesson 2.2 Note-Taking	Problem Set 2.1 Introduction to	The History of Springfield and Shelbyville



	Logarithms	
Lesson 2.3 Note-Taking	Properties of Logarithms Investigation	
Lesson 2.4 Note-Taking	Problem Set 2.2 Properties of Logarithmic Functions	
	Problem Set 2.3 Solving Logarithmic Equations	
	Problem Set 2.4 Applications of Logarithms	

### Unit 3: Polynomial Functions

AAL	AFL	AOL
Lesson 3.1 Note-Taking	Problem Set 3.1 Review of Distributive Law and Factoring	Video Conference with Teacher
Lesson 3.2 Note-Taking	Problem Set 3.2 Solving Quadratic Equations	Learning Log
Lesson 3.3 Note-Taking	Problem Set 3.3 Solving Factorable Polynomials	
Lesson 3.4 Note-Taking	Problem Set 3.4 Multiplicity and Sketching Polynomials	
Lesson 3.5 Note-Taking	Problem Set 3.5 Applications of Polynomials	
Lesson 3.6 Note-Taking	Problem Set 3.5 Identifying the Nature of the Function	

### Unit 4: Trigonometric Functions

AAL	AFL	AOL
Lesson 4.1 Note-Taking	Problem Set 4.1 Trigonometry Review and Basics	Virtual Conference with Teacher

Lesson 4.2 Note-Taking	Problem Set 4.2 Special Angles	Learning Log
Lesson 4.3 Note-Taking	Problem Set 4.3 Cast Rule	
Lesson 4.4 Note-Taking	Problem Set 4.4 Solving Trig Equations	
Lesson 4.5 Note-Taking	Problem Set 4.5 Trigonometry Problems in 2D	
Lesson 4.6 Note-Taking	Problem Set 4.6 Trigonometry Problems in 3D	
Lesson 4.7 Note-Taking	Problem Set 4.7 The Ambiguous Case of Sine Law	
Lesson 4.8 Note-Taking	Problem Set 4.8 Sinusoidal Functions	
Lesson 4.9 Note-Taking	Problem Set 4.9 Applications of Sinusoidal Functions	

### Unit 5: Vectors and Applications of Geometry

AAL	AFL	AOL
Lesson 5.1 Note-Taking	Problem Set 5.1 Vectors	Video Conference with Teacher
Lesson 5.2 Note-Taking	Problem Set 5.2 Vectors	Learning Log
Lesson 5.3 Note-Taking	Problem Set 5.3 Algebraic Vectors	Treasure Hunt
Lesson 5.4 Note-Taking	Problem 5.4 Applications of Vectors	
Lesson 5.5 Note-Taking	Problem Set 5.5 Circle Properties	
Lesson 5.6 Note-Taking	Problem Set 5.6 Arc Length and Sector Area	

Lesson 5.7 Note-Taking	Problem Set 5.7 Surface Area and Volume for Basic Geometric Shapes	
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## Finals

AOL
Culminating Activity

## CONSIDERATION FOR PROGRAM PLANNING

Students learn best when they are engaged in a variety of ways of learning. Guidance and career education courses lend themselves to a wide range of approaches in that they require students to research, think critically, work cooperatively, discuss relevant issues, and learn through practice in a variety of settings. Helping students become self-directed, lifelong learners is a fundamental aim of the guidance and career education curriculum. When students are engaged in active and experiential learning strategies, they tend to retain knowledge for longer periods and develop meaningful skills. Active and experiential learning strategies also enable students to apply their knowledge and skills to real-life issues and situations.

### ANTI-DISCRIMINATION EDUCATION IN GUIDANCE AND CAREER EDUCATION

Classroom teachers are the key educators of students who have special education needs. They have a responsibility to help all students learn, and they work collaboratively with special education teachers, where appropriate, to achieve this goal. Special Education Transformation: The Report of the Co-Chairs with the Recommendations of the Working Table on Special Education, 2006 endorses a set of beliefs that should guide program planning for students with special education needs in all disciplines. Those beliefs are as follows: All students can succeed. Universal design and differentiated instruction are effective and interconnected means of meeting the learning or productivity needs of any group of students. Successful instructional practices are founded on evidence-based research, tempered by experience.

### PROGRAM CONSIDERATIONS FOR ENGLISH LANGUAGE LEARNERS

Ontario schools have some of the most multilingual student populations in the world. The first language of approximately 20 percent of the students in Ontario's English language schools is a language other than English. Ontario's linguistic heritage includes several Aboriginal languages; many African, Asian, and European languages; and some varieties of English, such as Jamaican Creole. Many English language learners were born in Canada and raised in families and communities in which languages other than English were spoken, or in which the variety of English spoken differed significantly from the English of Ontario classrooms. Other English language learners arrive in Ontario as newcomers from other countries; they may have experience of highly sophisticated educational systems, or they may have

come from regions where access to formal schooling was limited. When they start school in Ontario, many of these students are entering a new linguistic and cultural environment.

### **THE ROLE OF TECHNOLOGY IN THE ENGLISH PROGRAM**

Information and communications technologies (ICT) provide a range of tools that can significantly extend and enrich teachers' instructional strategies and support students' language learning. ICT tools include multimedia resources, databases, Internet websites, digital cameras, and word-processing programs. Tools such as these can help students to collect, organize, and sort the data they gather and to write, edit, and present reports on their findings. Information and communications technologies can also be used to connect students to other schools, at home and abroad, and to bring the global community into the local classroom. Whenever appropriate, therefore, students should be encouraged to use ICT to support and communicate their learning.

### **ACCOMMODATIONS**

Accommodations will be based on meeting with parent, teachers, administration and external educational assessment report. The following three types of accommodations may be provided:

- Instructional accommodations:** such as changes in teaching strategies, including styles of presentation, methods of organization, or use of technology and multimedia.
- Environmental accommodations:** such as preferential seating or special lighting.
- Assessment accommodations:** such as allowing additional time to complete tests or assignments or permitting oral responses to test questions.

Other examples of modifications and aids, which may be used in this course, are:

- Provide step-by-step instructions.
- Help students create organizers for planning writing tasks.
- Record key words on the board or overhead when students are expected to make their own notes.
- Allow students to report verbally to a scribe (teacher/ student) who can help in note taking.
- Permit students a range of options for reading and writing tasks.
- Where an activity requires reading, provide it in advance.
- Provide opportunities for enrichment.